

# Detection and Diagnosis of Plant-wide Oscillations using the Spectral Envelope Method



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# Outline

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- Motivation
- Spectral Envelop Method and its use in Oscillation Detection & Variable Categorization
- Application to industrial data
- Conclusion
- Acknowledgement



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# Motivation

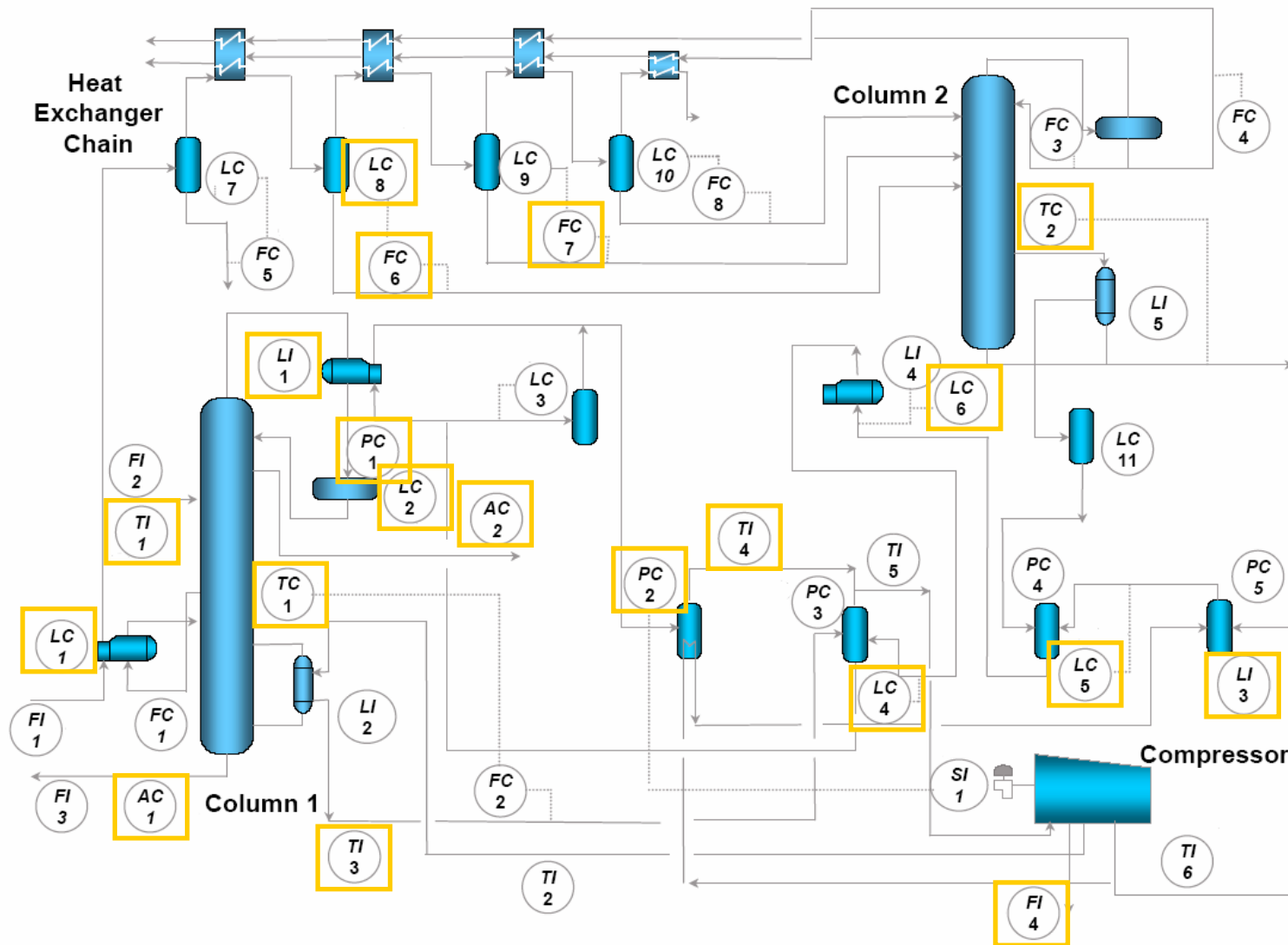


# Motivation

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- Oscillations are common in many processes, whose effects propagate to many units and thus may impact the overall process performance.
- For reasons of Safety and Profitability, it is important to detect and diagnose the plant-wide oscillation.

# Industrial Example





# Objective

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- Detect oscillations in the process variables.
- Categorize the variables that have similar oscillations.
- Deliver useful information on the potential root-cause(s)



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# Spectral Envelop Method and its use in Oscillation Detection & Variable Categorization

# Preliminaries

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- Assume  $\mathbf{X}(t) = \begin{bmatrix} \mathbf{x}_1(t) \\ \mathbf{x}_2(t) \\ \vdots \\ \mathbf{x}_m(t) \end{bmatrix}$  is an  $m$  dimensional, vector-valued time series, for  $-\infty < t < \infty$ .

- Denote  $g(t, \boldsymbol{\beta})$  as a linear combination of the variables of  $\mathbf{X}(t)$ :

$$g(t, \boldsymbol{\beta}) = \begin{bmatrix} \beta_1 & \beta_2 & \cdots & \beta_m \end{bmatrix} \begin{bmatrix} \mathbf{x}_1(t) \\ \mathbf{x}_2(t) \\ \vdots \\ \mathbf{x}_m(t) \end{bmatrix} = \boldsymbol{\beta}^T \mathbf{X}(t) \quad \text{with } \boldsymbol{\beta} = \begin{bmatrix} \beta_1 \\ \beta_2 \\ \vdots \\ \beta_m \end{bmatrix}$$

# Preliminaries (con't)

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- Denote the covariance of  $\mathbf{X}(t)$  as:

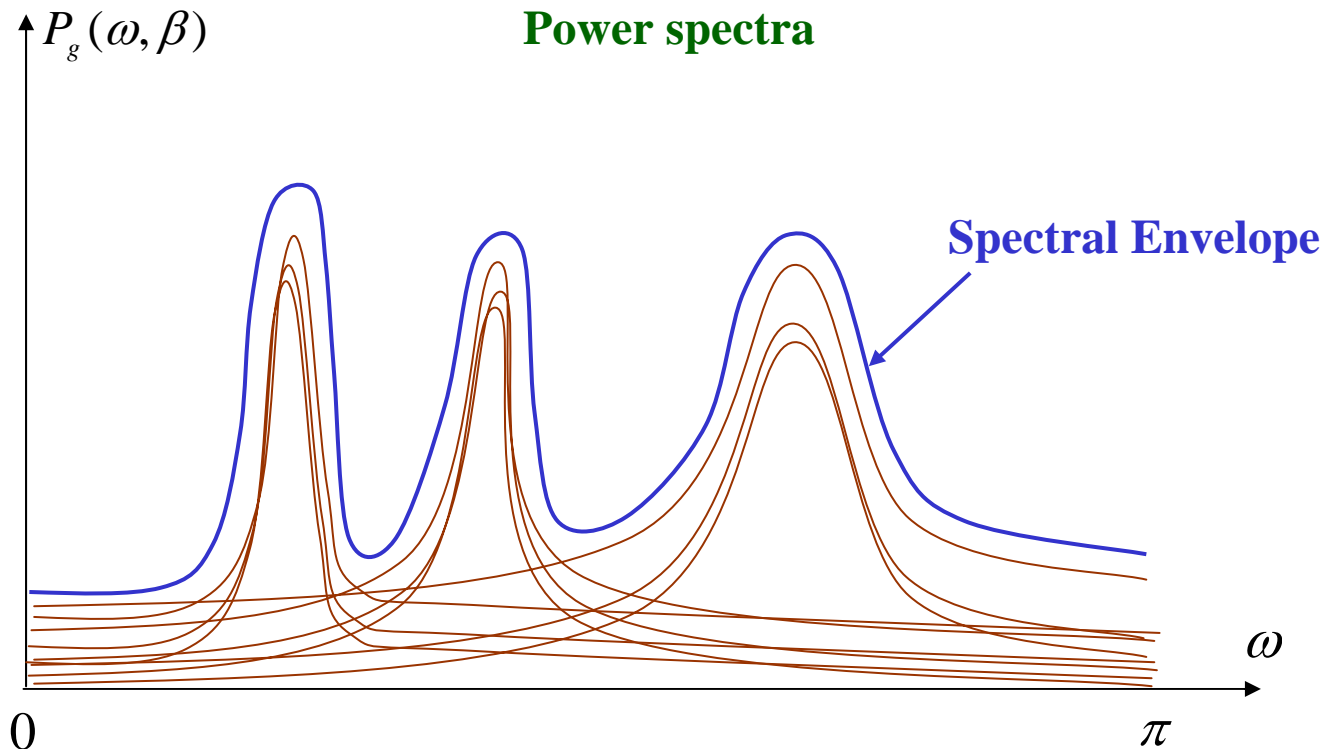
$$\mathbf{V}_{\mathbf{X}} = \text{Cov}(\mathbf{X}(t))$$

- The variance of  $g(t, \boldsymbol{\beta})$  can be expressed as:

$$V_g(\boldsymbol{\beta}) = \boldsymbol{\beta}^T \mathbf{V}_{\mathbf{X}} \boldsymbol{\beta}$$

# What is a Spectral Envelope?

- With the constraint that  $V_g(\beta) = \beta^T \mathbf{V}_X \beta = 1$  then  $g(t, \beta)$  is unit-variance.



# Definition of Spectral Envelop

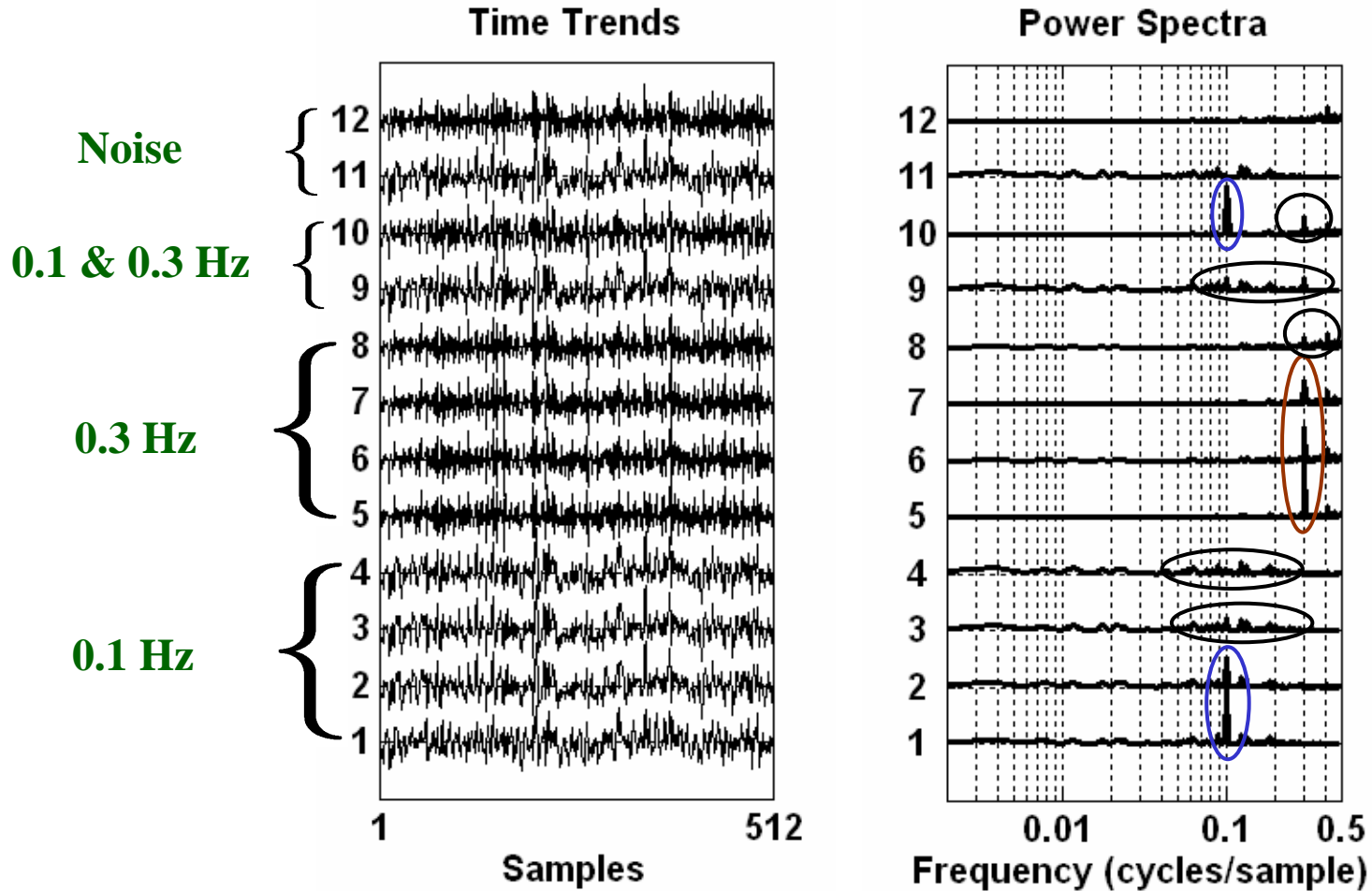
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- The Spectral Envelope of  $X(t)$  is defined to be

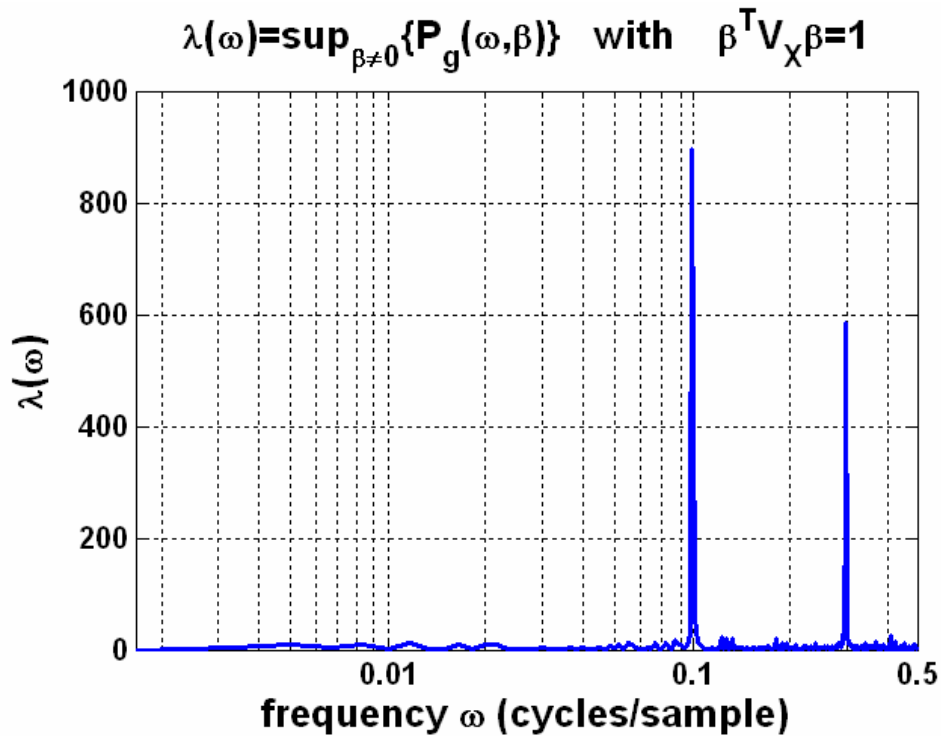
$$\begin{aligned}\lambda(\omega) &= \sup \{ \text{Power of the scaled series at frequency } \omega \} \\ &= \sup_{\beta \neq 0} \{ P_g(\omega, \beta) \} \quad \text{with} \quad \beta^T \mathbf{V}_X \beta = 1\end{aligned}$$

- The quantity  $\lambda(\omega)$  represents the largest power (variance) that can be obtained at frequency  $\omega$  for any unit-variance scaled series, which is a linear combination of the variables of  $\mathbf{X}(t)$  .

# Simulation example

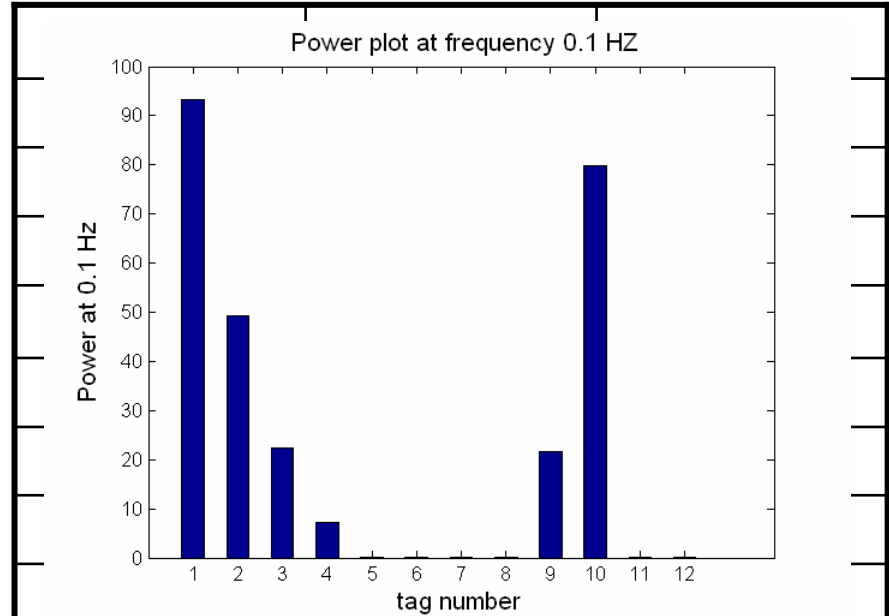
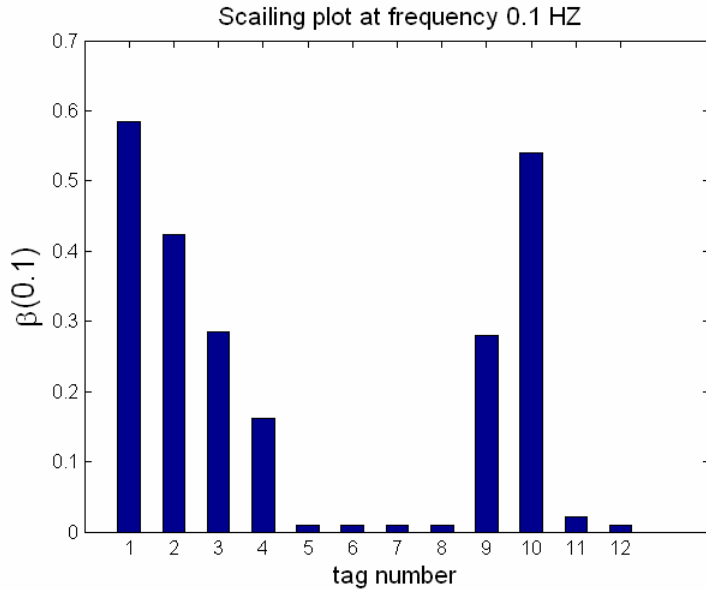


# Spectral Envelope



**Spectral envelope can identify the oscillations at 0.1 and 0.3 Hz.**

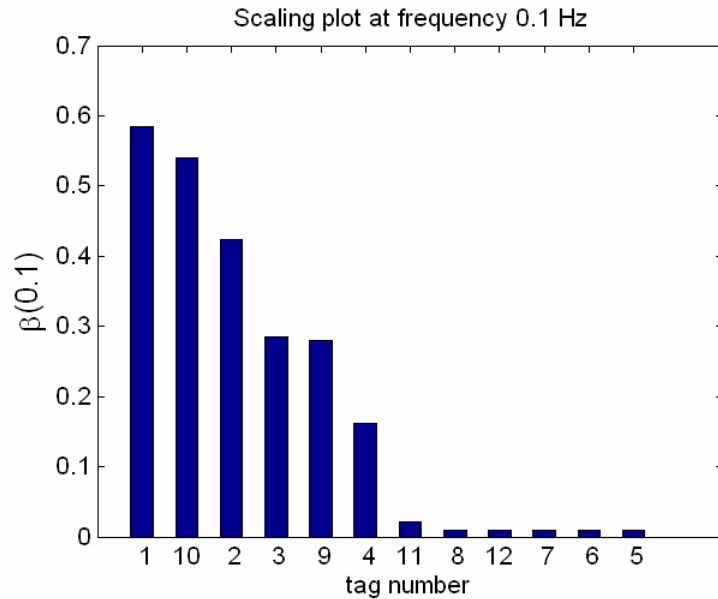
# Optimal Scalings at 0.1 Hz



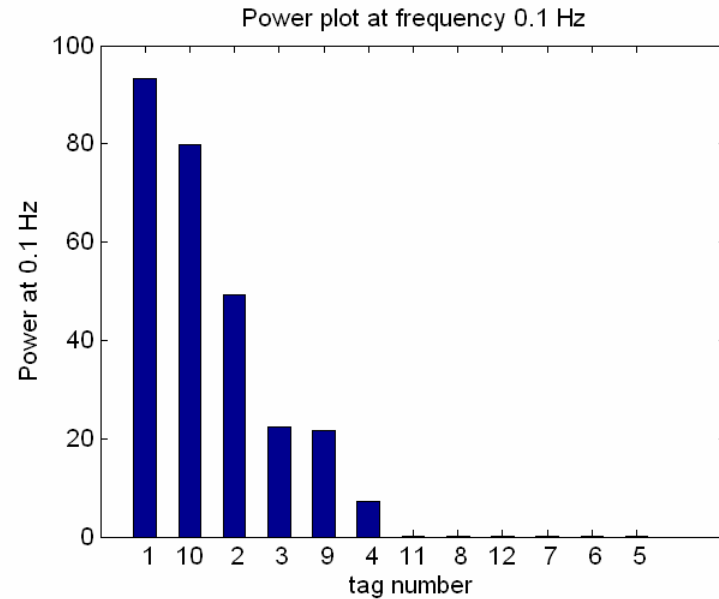
**Magnitude of scaling  
for each variable**

12	0.0093	0.0239
7	0.0092	0.0233
6	0.0089	0.0223
5	0.0088	0.0211

# Scaling plot *VS* Power plot at 0.1Hz



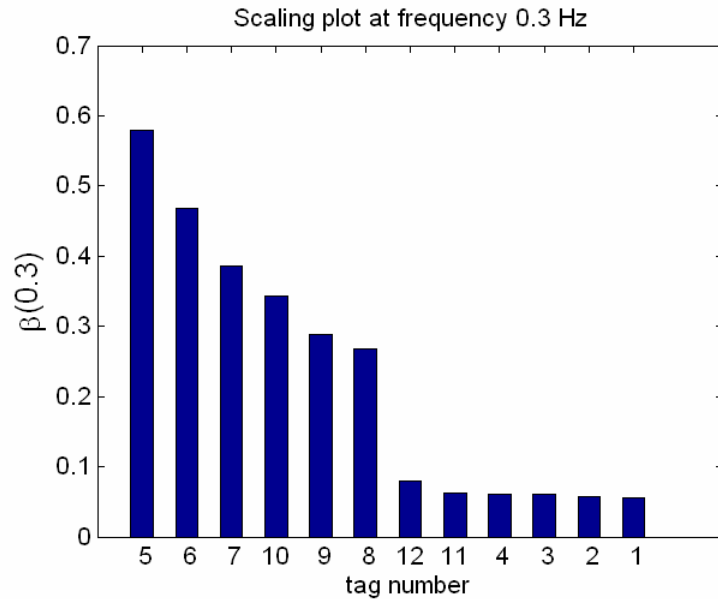
**Scaling plot**



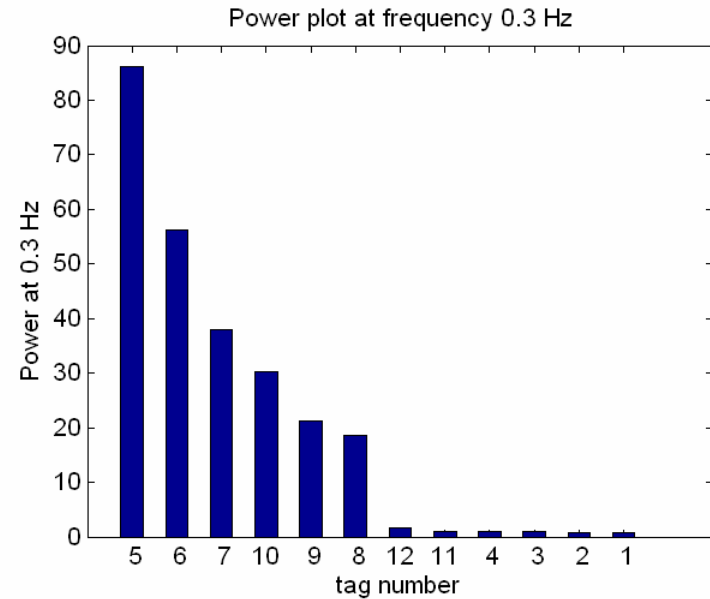
**Power plot**

Both plots can help us to categorize variables.

# Scaling plot *VS* Power plot at 0.3Hz



**Scaling plot**



**Power plot**

Both plots can help us to categorize variables.



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# Application to industrial data



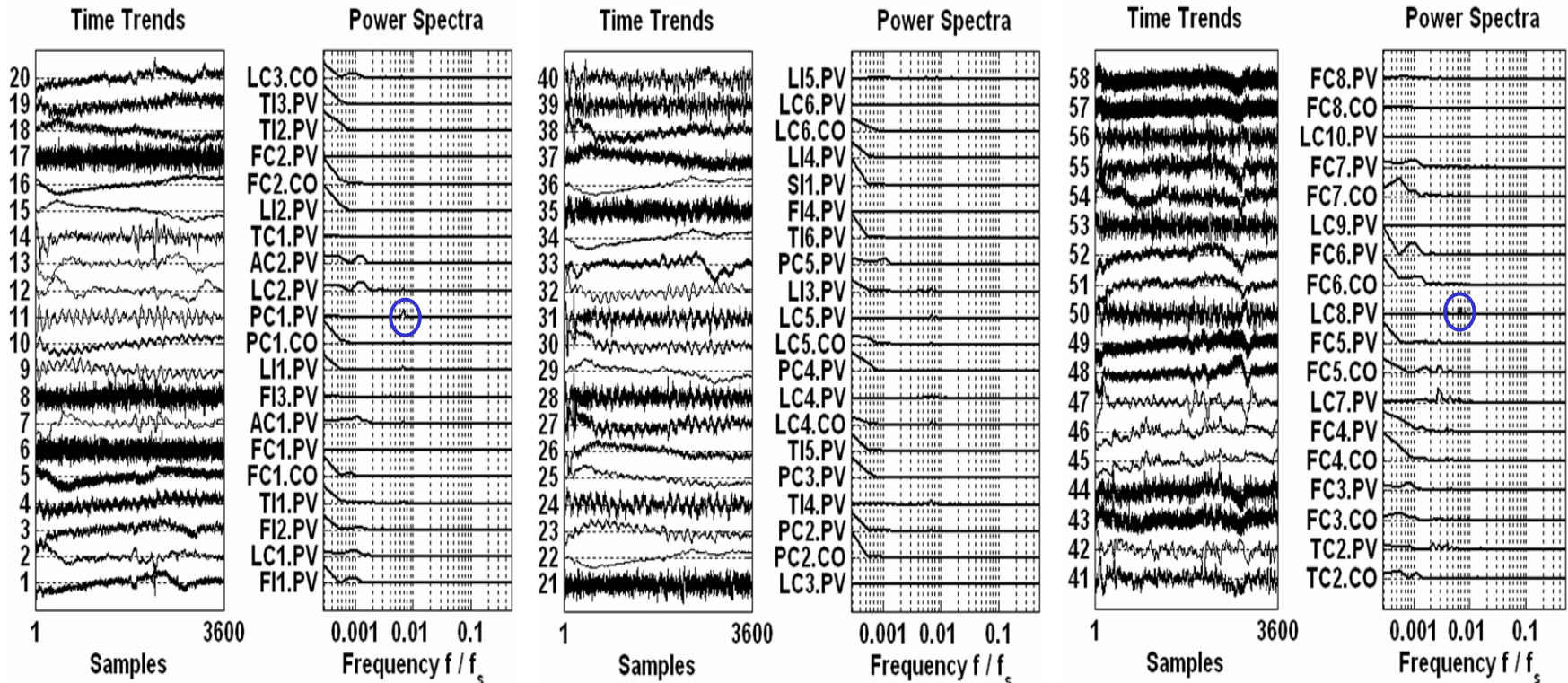
# Distillation plant example

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- Data from Mitsubishi Chemical Corporation
- 58 process variables from a distillation plant
- 3600 observations sampled at 1 min interval

# Overview of the data

Interested in oscillations with period 2.5 hours  
 ( about 150 samples/cycle, or  $1/150 = 0.0067$  )

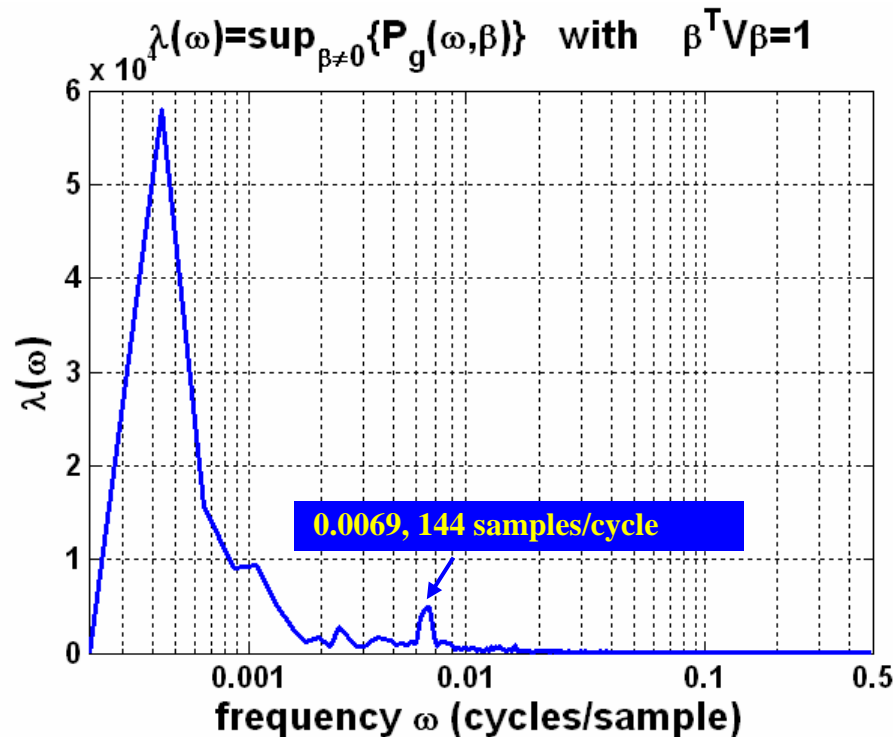


tag 1- 20

tag 21- 40

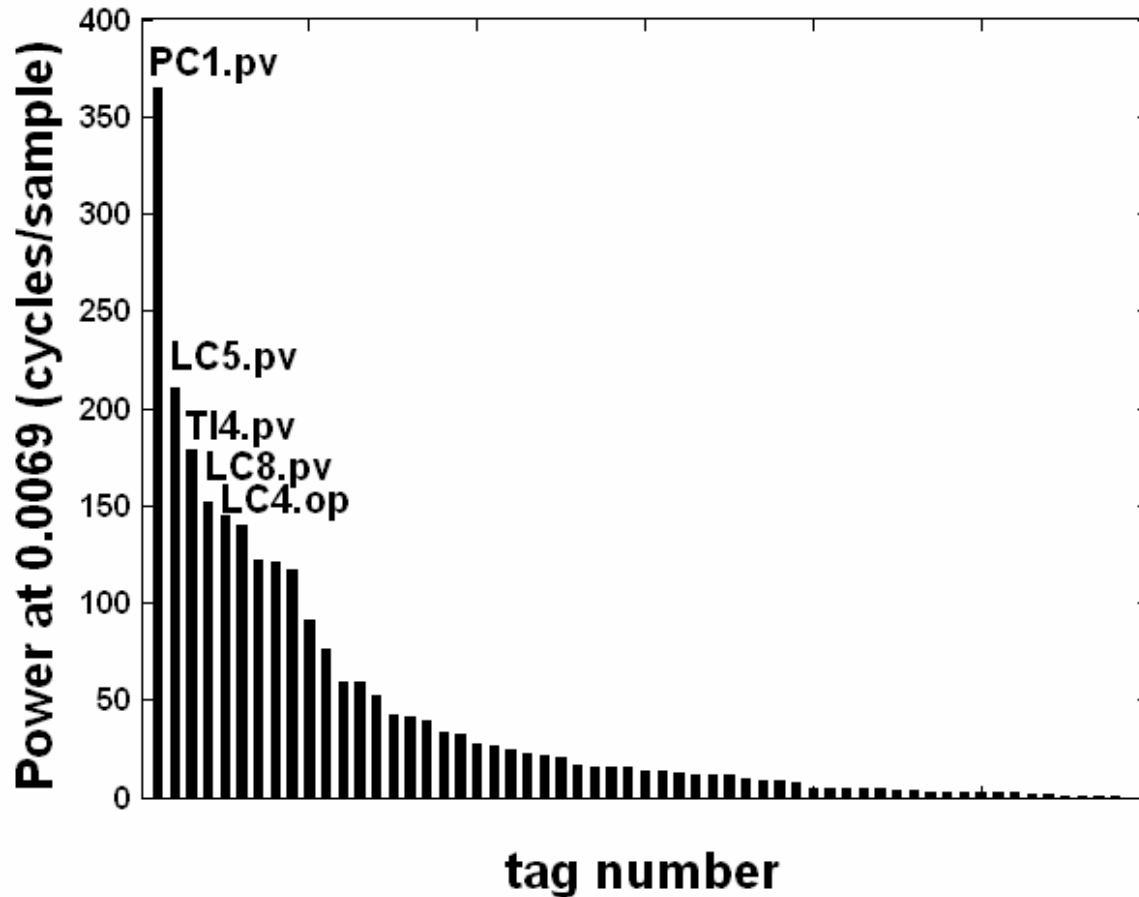
tag 41- 58

# Spectral Envelope



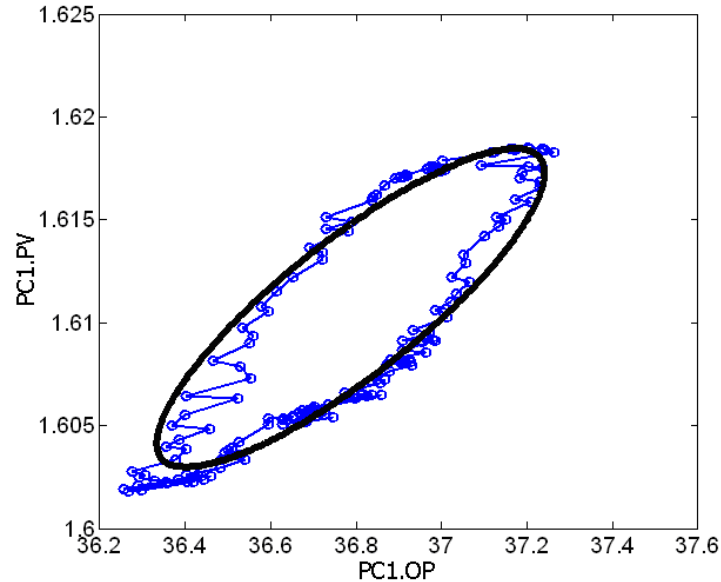
**Spectral envelope detect the oscillation of concern with a period of 144 samples/cycle.**

# Power plot at 0.0069 (144 samples/cycle)



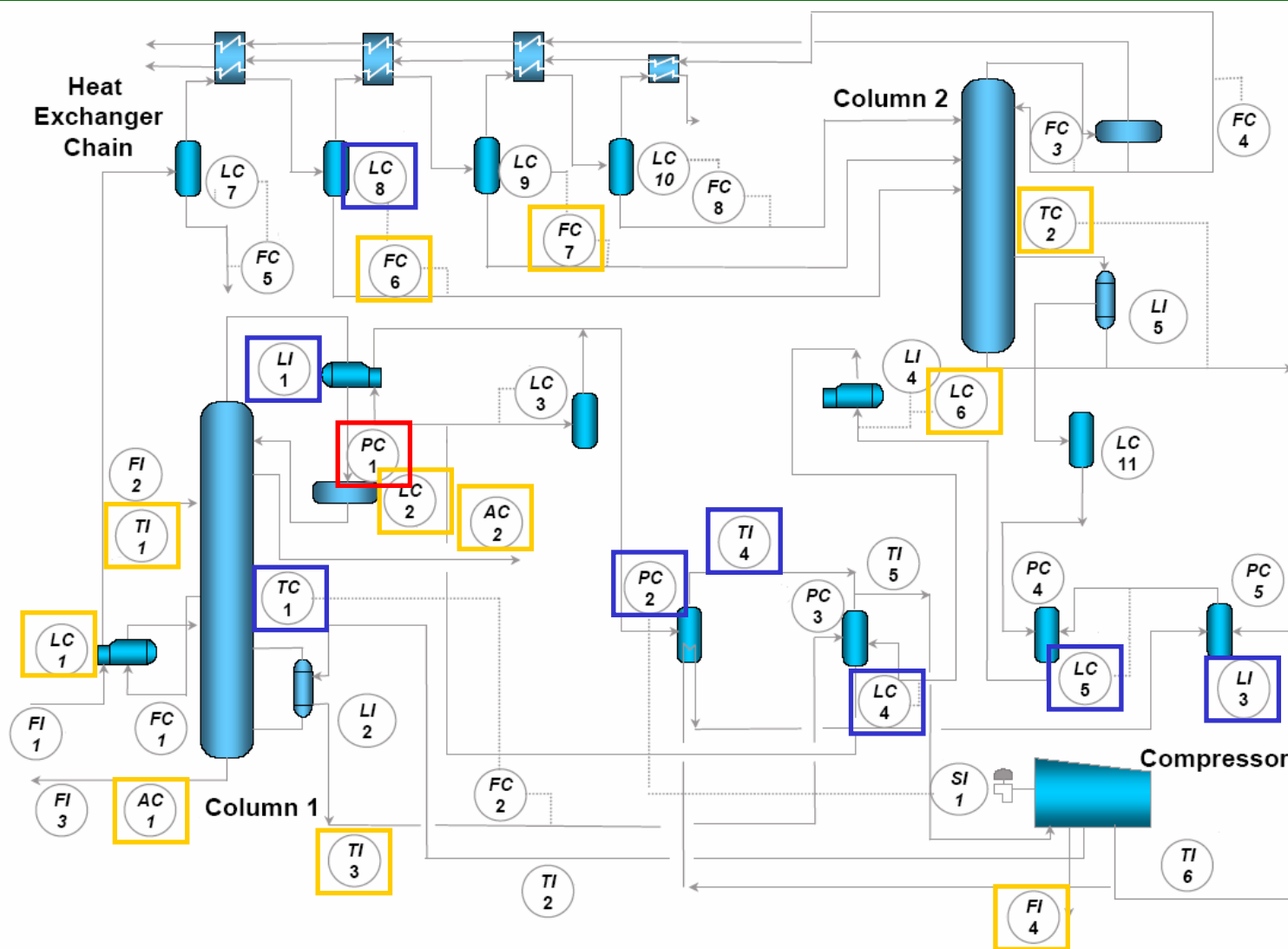
**Power plot**

# *pV-op* plot



1. This plot shows a pattern of valve stiction.
2. Simple closed-loop plant test had confirmed that the valve really has stiction problem.
3. Further plant test and maintenance has been scheduled during the next plant shutdown.

# Root cause Diagnosis





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# Conclusion

# Conclusion

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- Spectral Envelop (SE) method has been successfully applied to industrial data to identify the oscillation frequencies and categorize the variables that have the same oscillations.
- Scaling plot and power plot provide useful information on the root-cause of oscillations.



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# Acknowledgement

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Thank you!